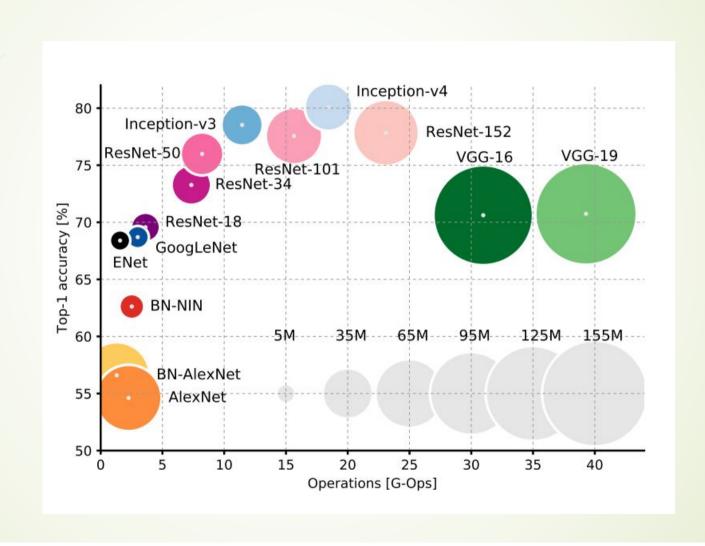


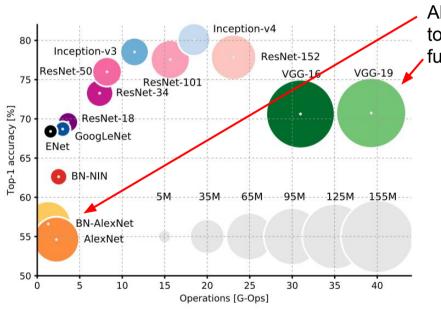
### Recurrent Neural Networks (RNN) and Long-Short-Term-Memory (LSTM)

Yuan YAO HKUST

#### Summary

- We have shown:
  - First order optimization methods: GD (BP), SGD, Nesterov, Adagrad, ADAM, RMSPROP, etc.
  - Second order optimization methods: L-BFGS
  - Regularization methods: Penalty (L2/L1/Elastic), Dropout, Batch Normalization, Data Augmentation, etc.
  - CNN Architectures: LeNet5, Alexnet, VGG, GoogleNet, Resnet
- Now
  - Recurrent Neural Networks
  - LSTM
- Reference:
  - ► Feifei Li, Stanford cs231n





AlexNet and VGG have tons of parameters in the fully connected layers

AlexNet: ~62M parameters

FC6: 256x6x6 -> 4096: 38M params

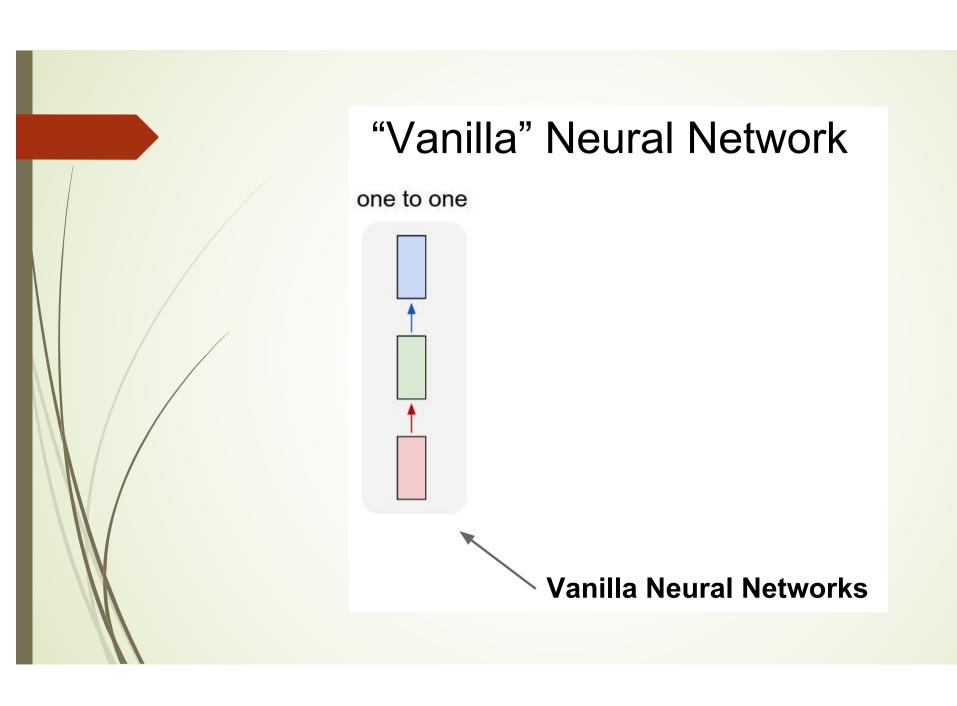
FC7: 4096 -> 4096: 17M params

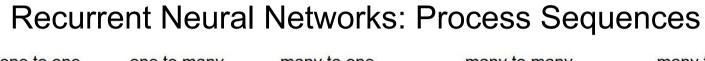
FC8: 4096 -> 1000: 4M params

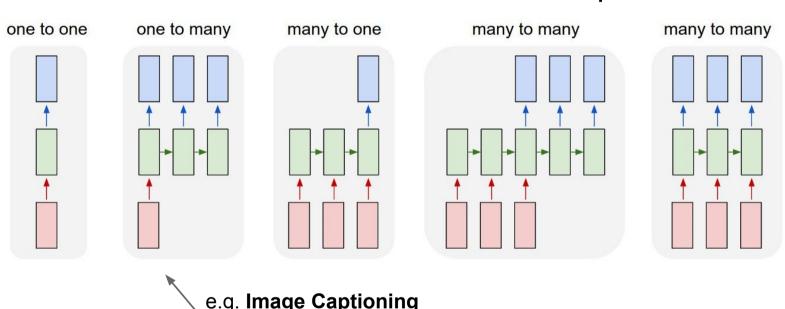
~59M params in FC layers!

ResNet allows deep networks with small number of params.

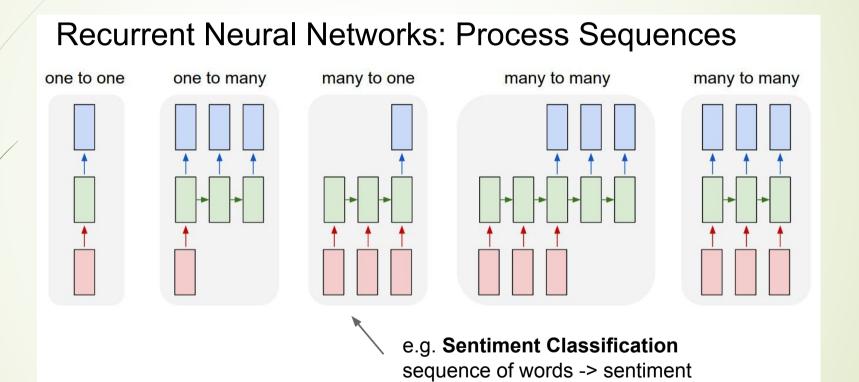
# Recurrent Neural Networks



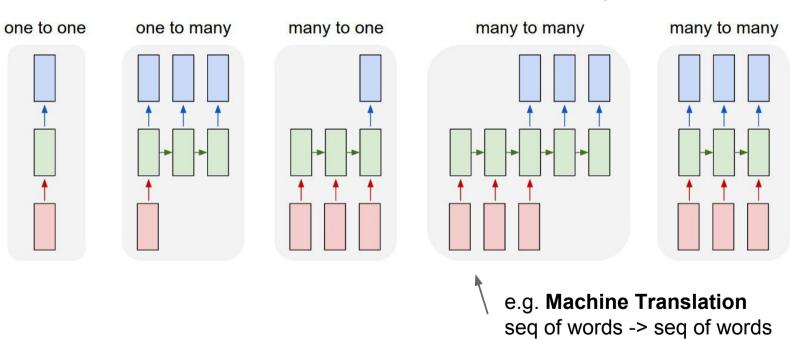


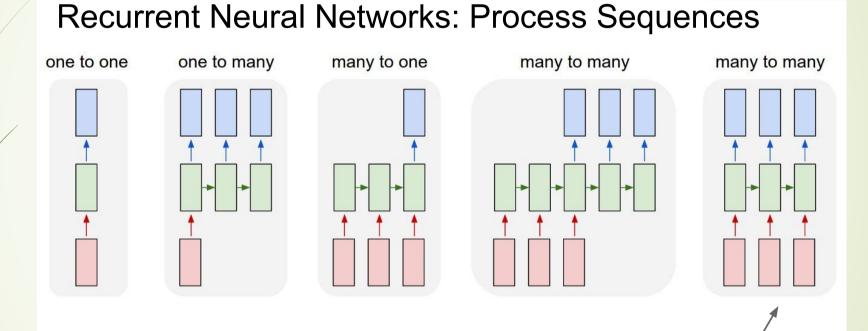


e.g. **Image Captioning** image -> sequence of words









e.g. Video classification on frame level

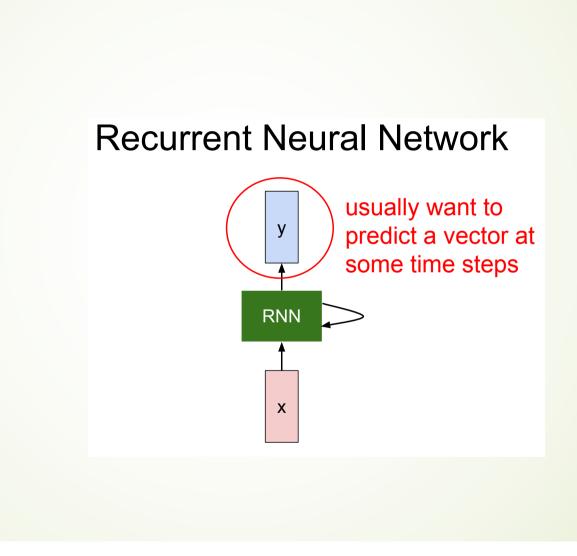
#### Sequential Processing of Non-Sequence Data

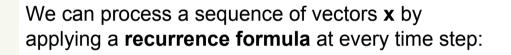
Classify images by taking a series of "glimpses"

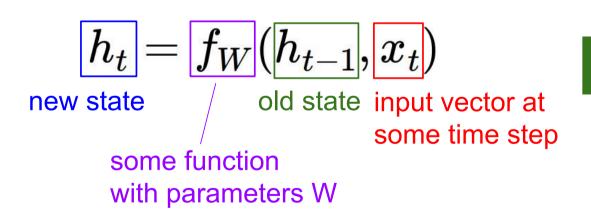


Ba, Mnih, and Kavukcuoglu, "Multiple Object Recognition with Visual Attention", ICLR 2015.
Gregor et al, "DRAW: A Recurrent Neural Network For Image Generation", ICML 2015
Figure copyright Karol Gregor, Ivo Danihelka, Alex Graves, Danilo Jimenez Rezende, and Daan Wierstra, 2015. Reproduced with neuroscion

# Recurrent Neural Network RNN







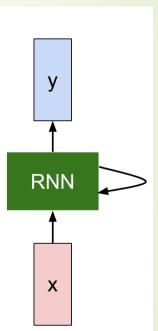
RNN

Χ

We can process a sequence of vectors **x** by applying a **recurrence formula** at every time step:

$$h_t = f_W(h_{t-1}, x_t)$$

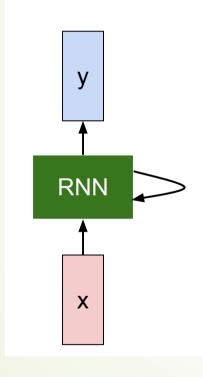
Notice: the same function and the same set of parameters are used at every time step.



#### Vanilla Recurrent Neural Networks

State Space equations in feedback dynamical systems

The state consists of a single "hidden" vector **h**:



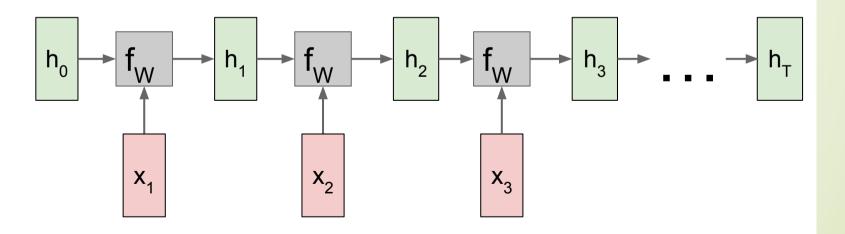
$$h_t = f_W(h_{t-1}, x_t)$$

$$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t)$$

$$y_t = W_{hy} h_t$$

or, 
$$y_t = \operatorname{softmax}(W_{hy}h_t)$$

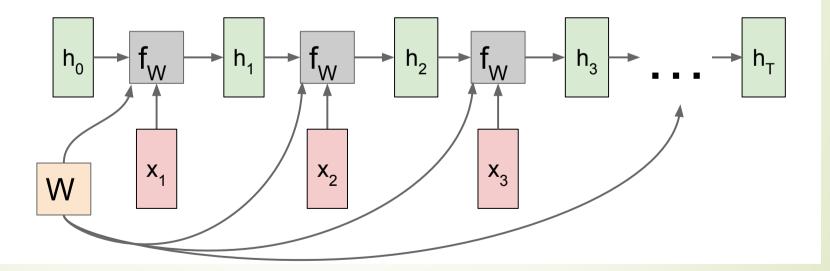
#### RNN: Computational Graph



#### Time invariant systems

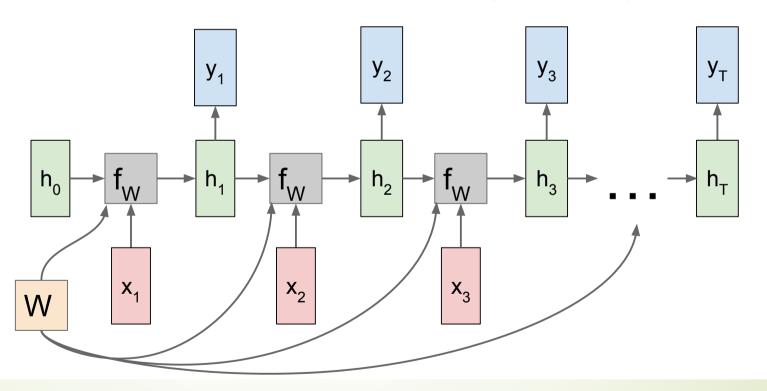
#### **RNN: Computational Graph**

Re-use the same weight matrix at every time-step

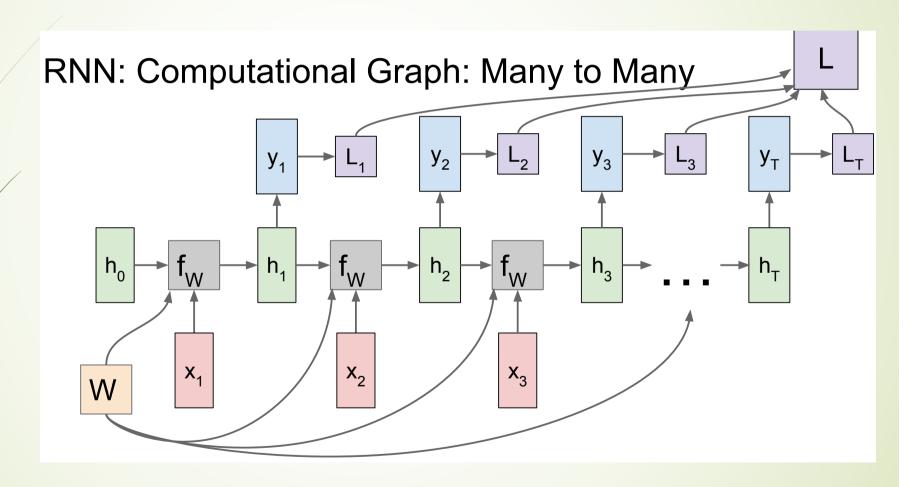


#### Outputs added

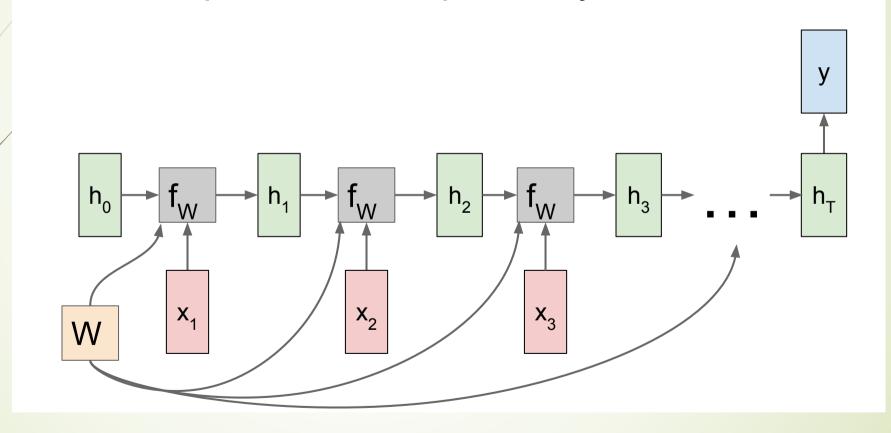




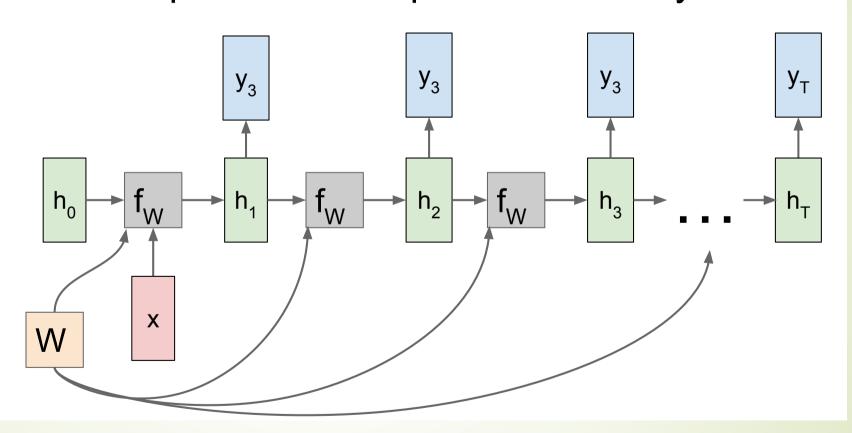
#### Loss modules



#### RNN: Computational Graph: Many to One

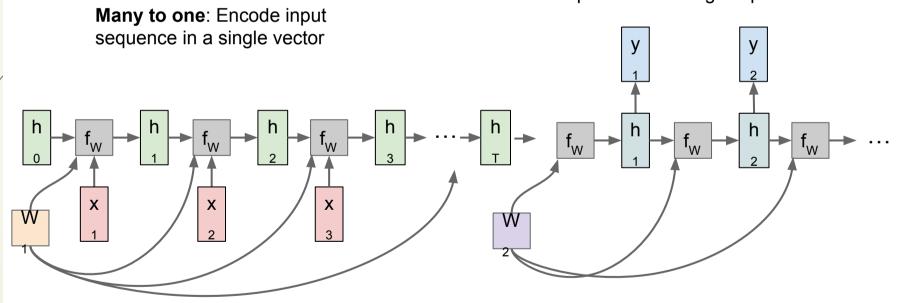


#### RNN: Computational Graph: One to Many



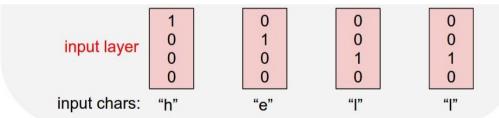
#### Sequence to Sequence: Many-to-one + one-to-many

One to many: Produce output sequence from single input vector



Vocabulary: [h,e,l,o]

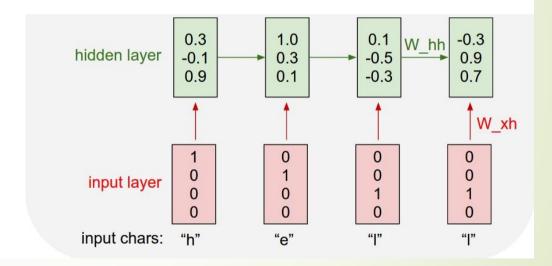
Example training sequence: "hello"



 $h_t = anh(W_{hh}h_{t-1} + W_{xh}x_t)$ 

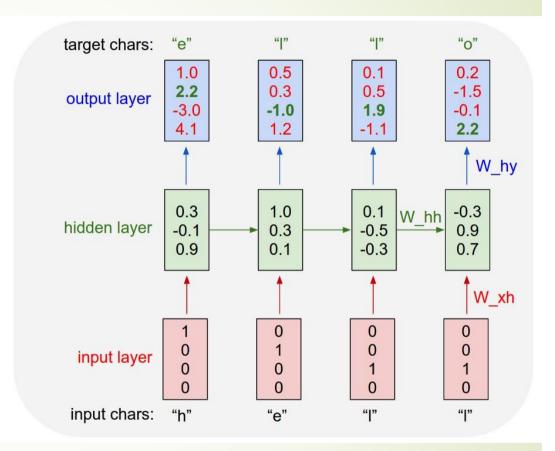
Vocabulary: [h,e,l,o]

Example training sequence: "hello"

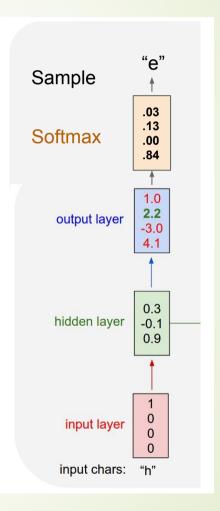


Vocabulary: [h,e,l,o]

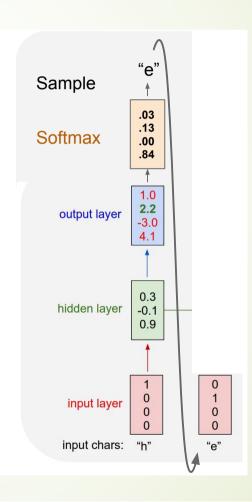
Example training sequence: "hello"



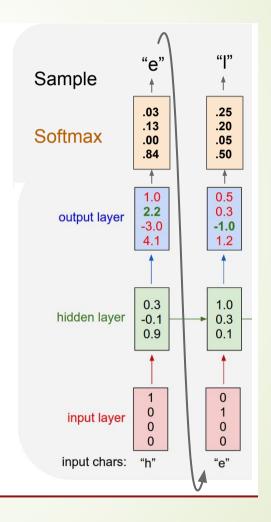
Vocabulary: [h,e,l,o]



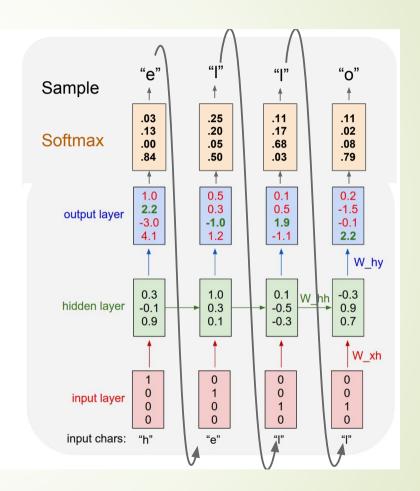
Vocabulary: [h,e,l,o]

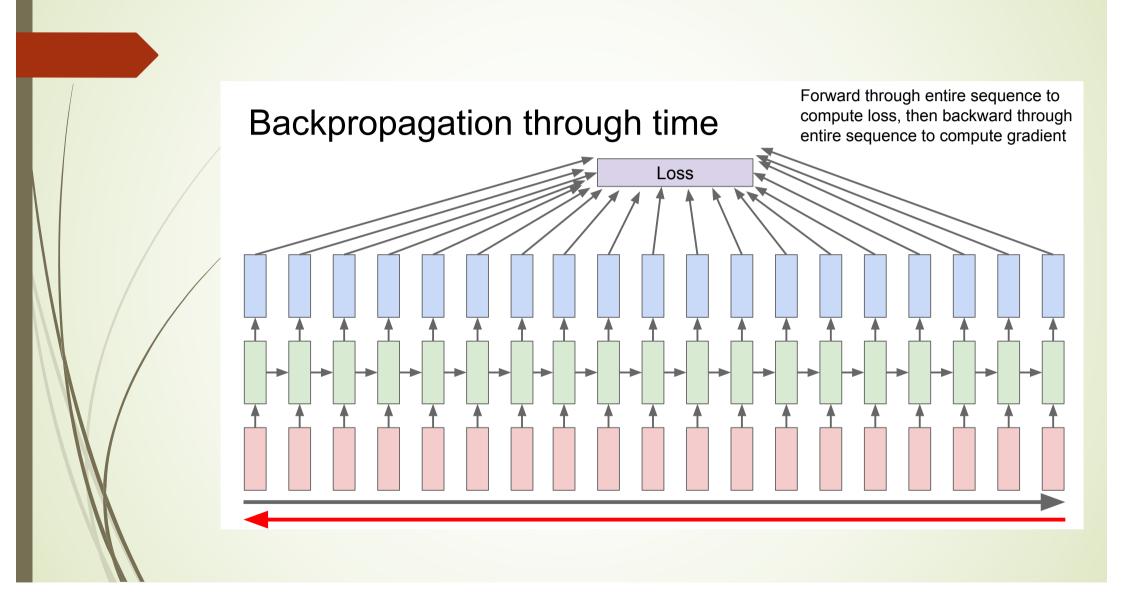


Vocabulary: [h,e,l,o]

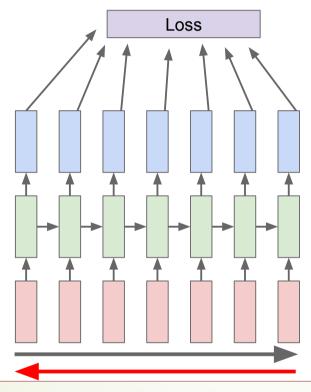


Vocabulary: [h,e,l,o]



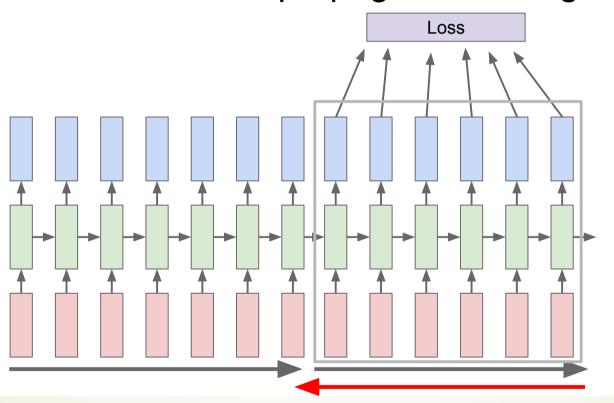




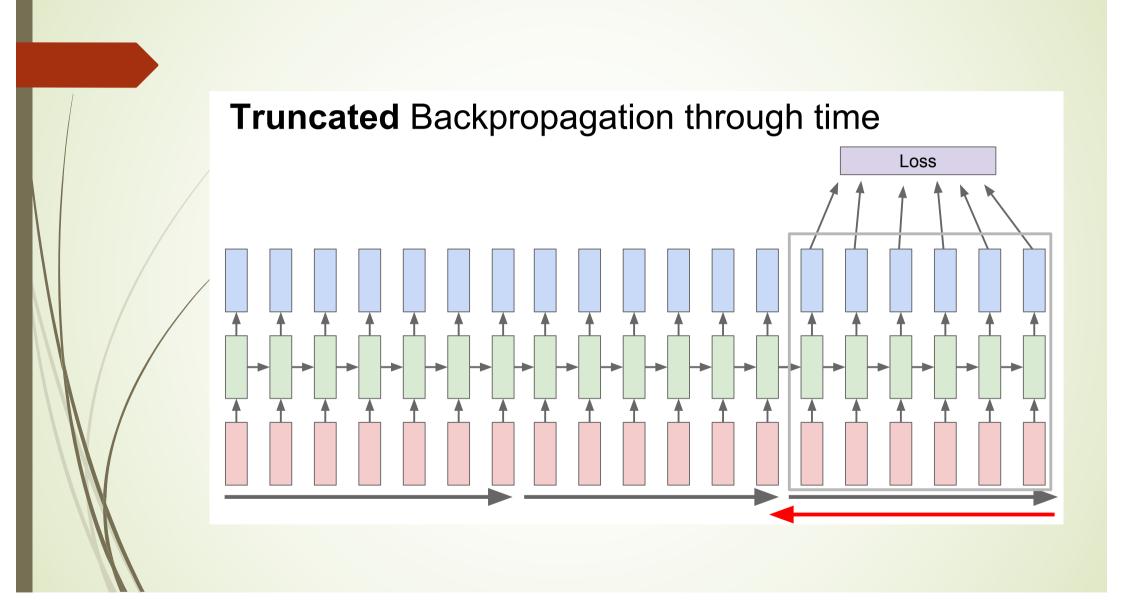


Run forward and backward through chunks of the sequence instead of whole sequence





Carry hidden states forward in time forever, but only backpropagate for some smaller number of steps



#### Example: Text->RNN

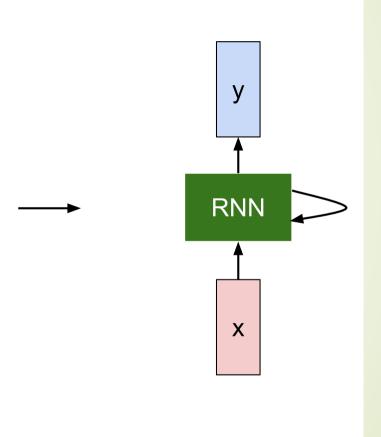
#### THE SONNETS

#### by William Shakespeare

From fairest creatures we desire increase, That thereby beauty's rose might never die, But as the riper should by time decease, His tender heir might bear his memory: But thou, contracted to thine own bright eyes, Feed'st thy light's flame with self-substantial fuel, Making a famine where abundance lies, Thyself thy foe, to thy sweet self too cruel: Thou that art now the world's fresh ornament, And only herald to the gaudy spring, Within thine own bud buriest thy content. And tender churl mak'st waste in niggarding: Pity the world, or else this glutton be, To eat the world's due, by the grave and thee.

When forty winters shall besiege thy brow, And dig deep trenches in thy beauty's field, Thy youth's proud livery so gazed on now, Will be a tatter'd weed of small worth held: Then being asked, where all thy beauty lies. Where all the treasure of thy lusty days; To say, within thine own deep sunken eyes, Were an all-eating shame, and thriftless praise. How much more praise deserv'd thy beauty's use, If thou couldst answer 'This fair child of mine Shall sum my count, and make my old excuse.' Proving his beauty by succession thine! This were to be new made when thou art old,

And see thy blood warm when thou feel'st it cold.



https://gist.github.com/karpathy/d4dee566867f8291f086



tyntd-iafhatawiaoihrdemot lytdws e ,tfti, astai f ogoh eoase rrranbyne 'nhthnee e plia tklrgd t o idoe ns,smtt h ne etie h,hregtrs nigtike,aoaenns lng

#### train more

"Tmont thithey" fomesscerliund Keushey. Thom here sheulke, anmerenith ol sivh I lalterthend Bleipile shuwy fil on aseterlome coaniogennc Phe lism thond hon at. MeiDimorotion in ther thize."

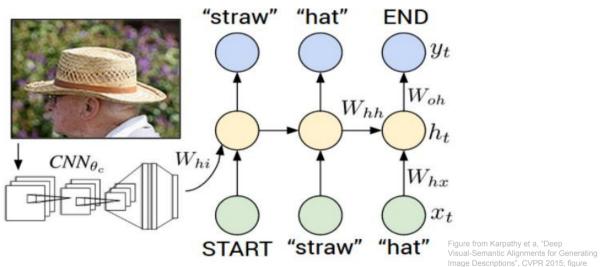
#### train more

Aftair fall unsuch that the hall for Prince Velzonski's that me of her hearly, and behs to so arwage fiving were to it beloge, pavu say falling misfort how, and Gogition is so overelical and ofter.

#### train more

"Why do what that day," replied Natasha, and wishing to himself the fact the princess, Princess Mary was easier, fed in had oftened him. Pierre aking his soul came to the packs and drove up his father-in-law women.

# Image Captioning

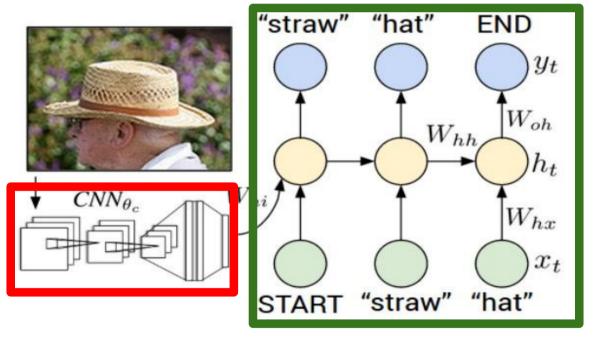


Explain Images with Multimodal Recurrent Neural Networks, Mao et al.

Deep Visual-Semantic Alignments for Generating Image Descriptions, Karpathy and Fei-Fei Show and Tell: A Neural Image Caption Generator, Vinyals et al.

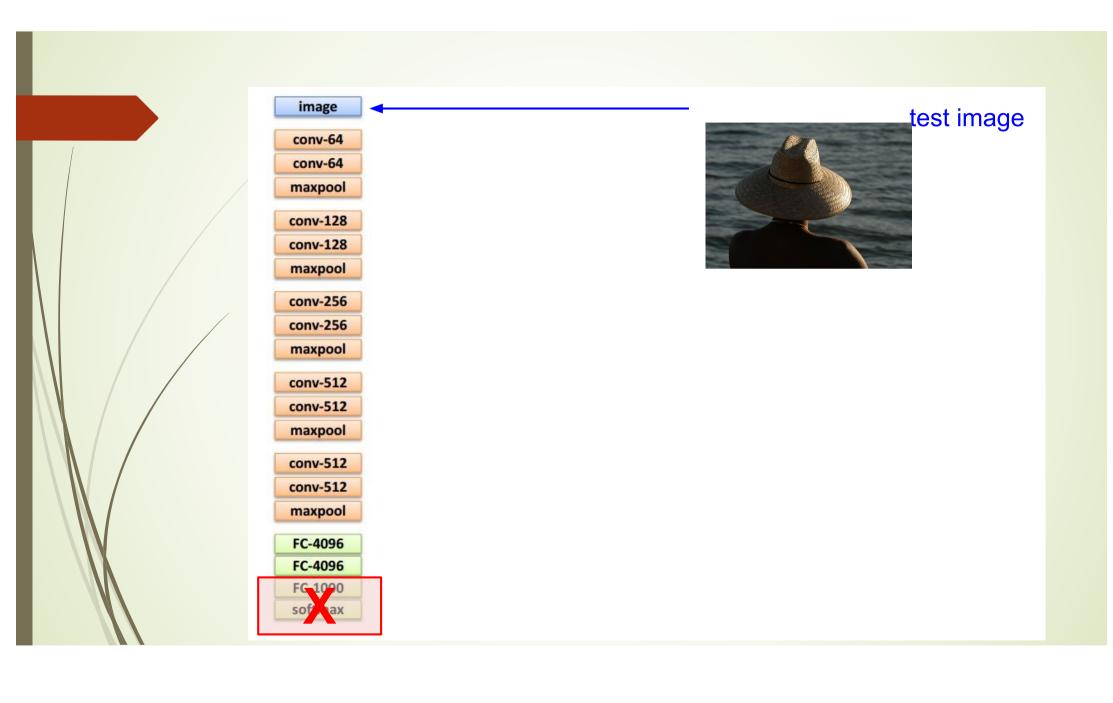
Long-term Recurrent Convolutional Networks for Visual Recognition and Description, Donahue et al. Learning a Recurrent Visual Representation for Image Caption Generation, Chen and Zitnick

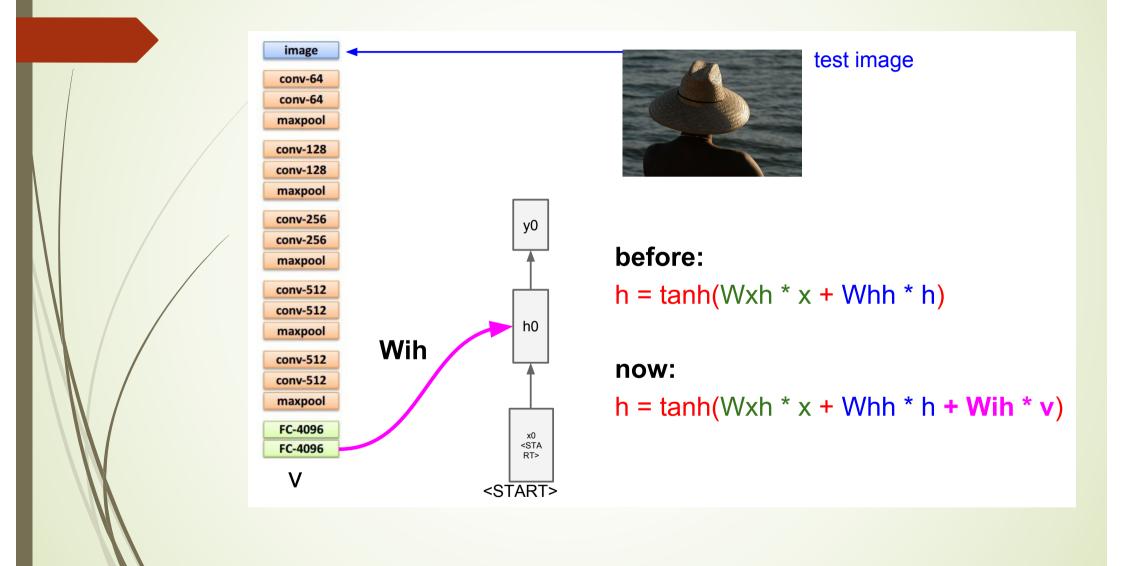
# **Recurrent Neural Network**

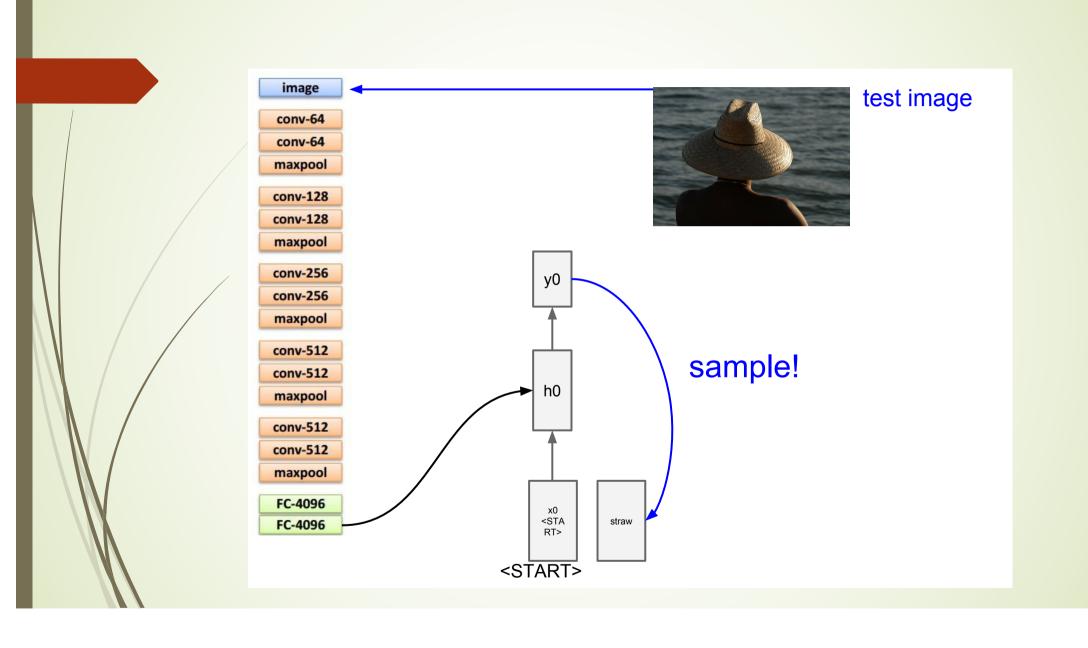


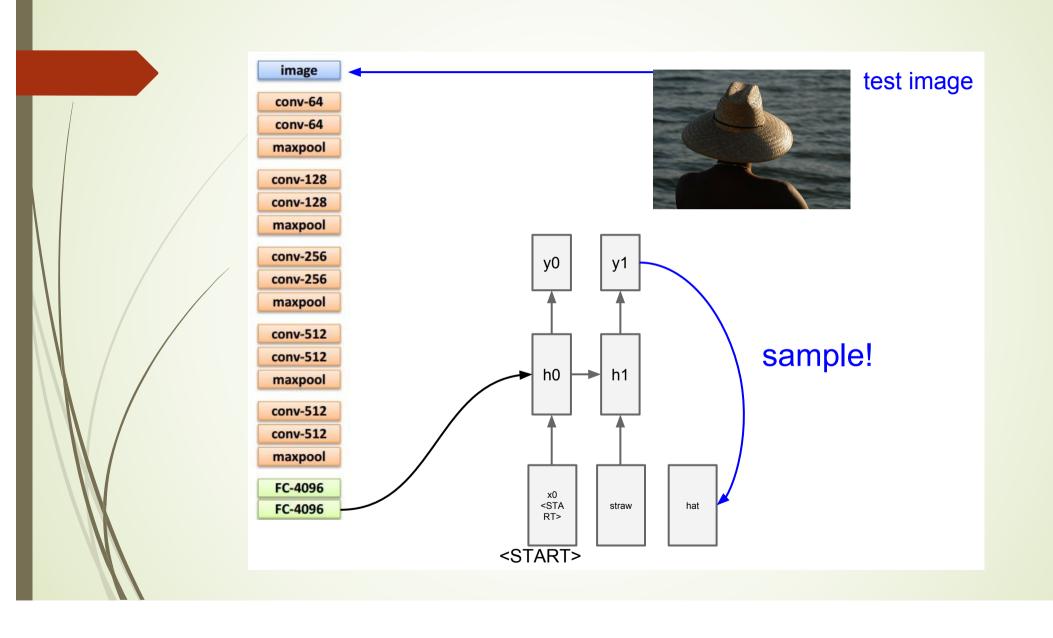
**Convolutional Neural Network** 

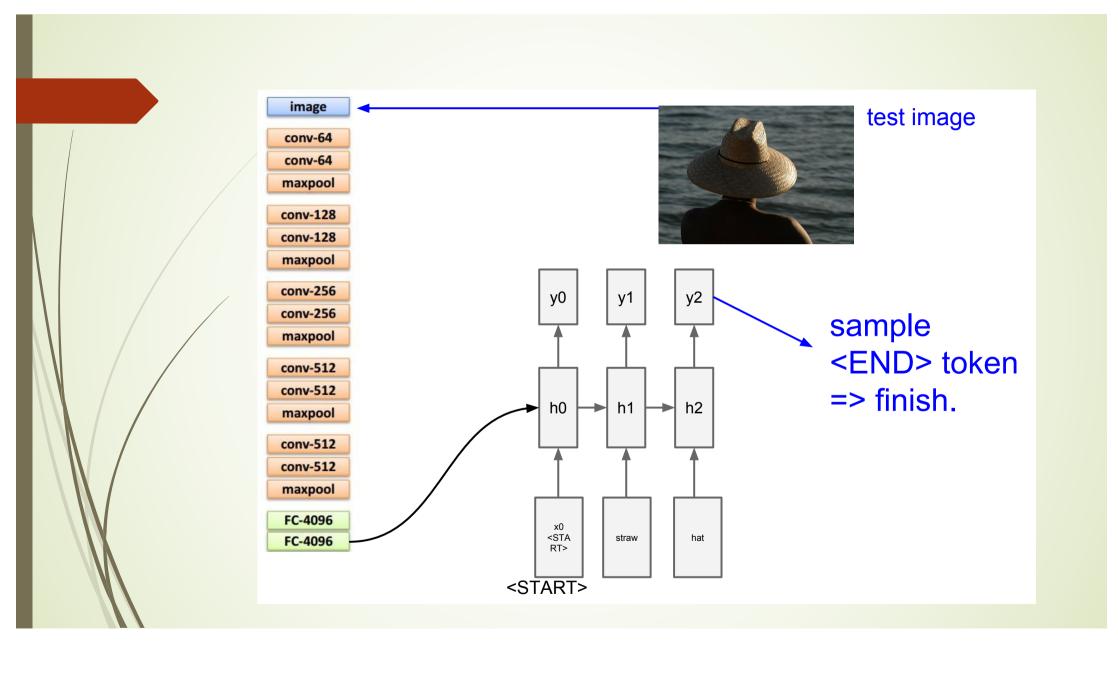












# Image Captioning: Example Results

Captions generated using <u>neuraltalk2</u>
All images are <u>CC0 Public domain</u>:
<u>cat suitcase</u>, <u>cat tree</u>, <u>dog</u>, <u>bear</u>,
<u>surfers</u>, <u>tennis</u>, <u>giraffe</u>, <u>motorcycle</u>



A cat sitting on a suitcase on the floor



A cat is sitting on a tree branch



A dog is running in the grass with a frisbee



A white teddy bear sitting in the grass



Two people walking on the beach with surfboards



A tennis player in action on the court



Two giraffes standing in a grassy field



A man riding a dirt bike on a dirt track

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 10 - 75 May 4, 2017

#### Captions generated using neuraltalk2 All images are CC0 Public domain: fur coat. handstand. spider web. baseball

# Image Captioning: Failure Cases



A woman is holding a cat in her hand



A person holding a computer mouse on a desk



A woman standing on a beach holding a surfboard



A bird is perched on a tree branch

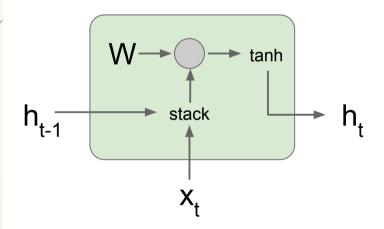


A man in a baseball uniform throwing a ball

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 10 - 76 May 4, 2017

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



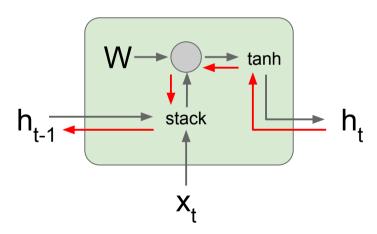
$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$

$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

$$= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Backpropagation from  $h_t$  to  $h_{t-1}$  multiplies by W (actually  $W_{hh}^{T}$ )

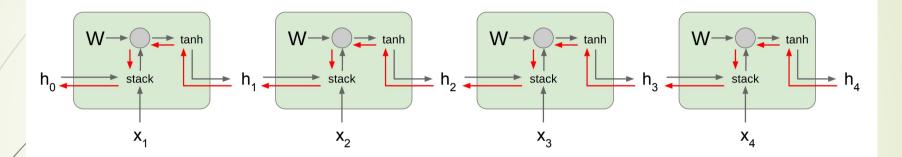


$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$

$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

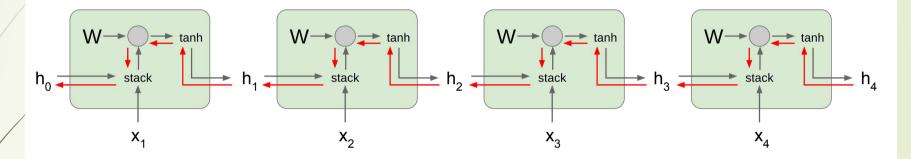
$$= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



Computing gradient of h<sub>0</sub> involves many factors of W (and repeated tanh)

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



Computing gradient of h<sub>0</sub> involves many factors of W (and repeated tanh)

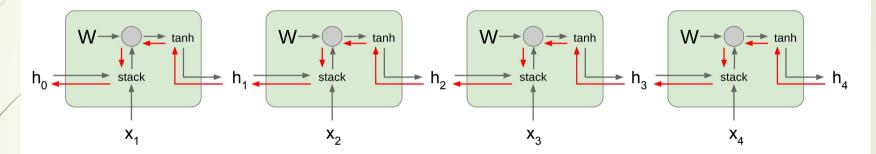
Largest singular value > 1:

**Exploding gradients** 

Largest singular value < 1:

**Vanishing gradients** 

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



Computing gradient of h<sub>0</sub> involves many factors of W (and repeated tanh)

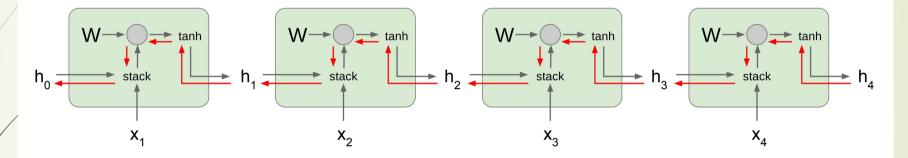
Largest singular value > 1: **Exploding gradients** 

Largest singular value < 1: **Vanishing gradients** 

Gradient clipping: Scale gradient if its norm is too big

```
grad_norm = np.sum(grad * grad)
if grad_norm > threshold:
   grad *= (threshold / grad_norm)
```

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



Computing gradient of h<sub>0</sub> involves many factors of W (and repeated tanh)

Largest singular value > 1: **Exploding gradients** 

Largest singular value < 1: Vanishing gradients 

← Cha

Change RNN architecture

# Long Short Term Memory (LSTM)

# Long Short Term Memory (LSTM)

#### Vanilla RNN

$$h_t = \tanh\left(W\begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right)$$

#### **LSTM**

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$
$$c_t = f \odot c_{t-1} + i \odot g$$
$$h_t = o \odot \tanh(c_t)$$

Hochreiter and Schmidhuber, "Long Short Term Memory", Neural Computation



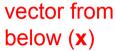
[Hochreiter et al., 1997]

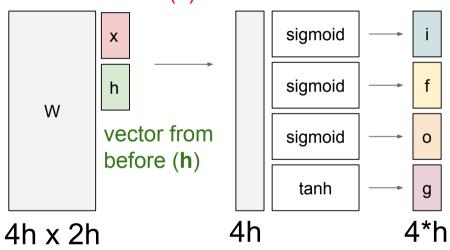
f: Forget gate, Whether to erase cell

i: Input gate, whether to write to cell

g: Gate gate (?), How much to write to cell

**o**: Output gate, How much to reveal cell



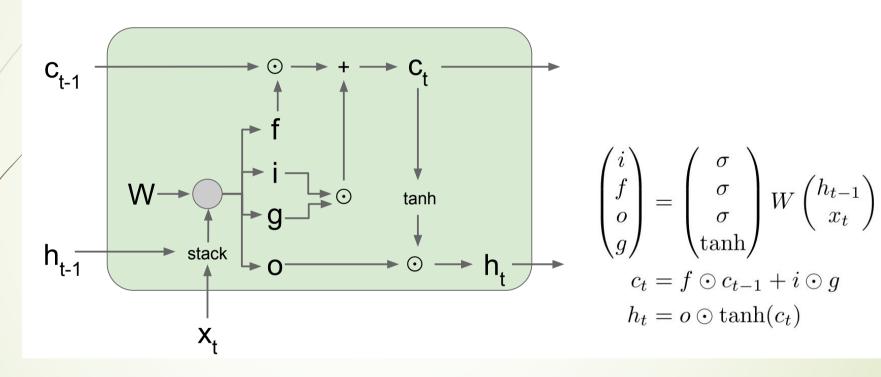


$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$
$$h_t = o \odot \tanh(c_t)$$

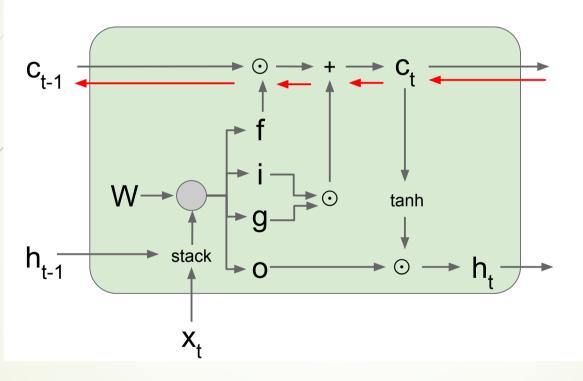
#### Long Short Term Memory (LSTM)

[Hochreiter et al., 1997]



### Long Short Term Memory (LSTM): Gradient Flow

[Hochreiter et al., 1997]

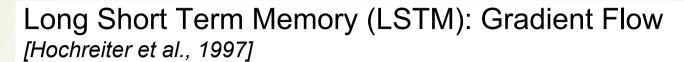


Backpropagation from c<sub>t</sub> to c<sub>t-1</sub> only elementwise multiplication by f, no matrix multiply by W

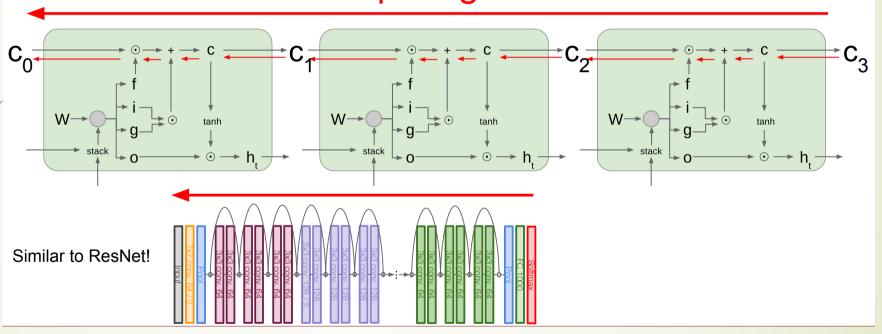
$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

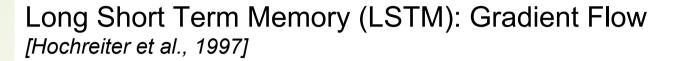
$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

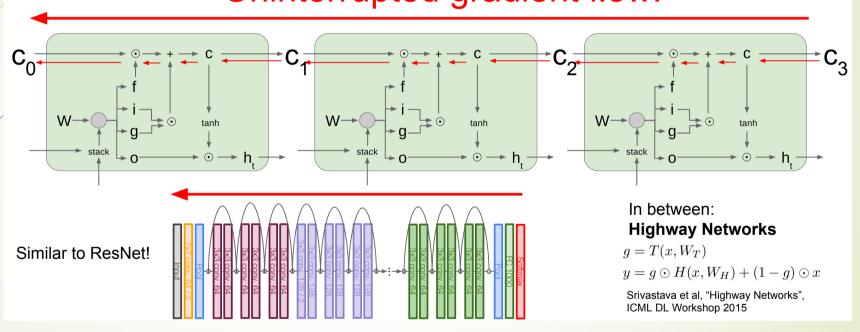


# Uninterrupted gradient flow!





# Uninterrupted gradient flow!



#### Multilayer RNNs

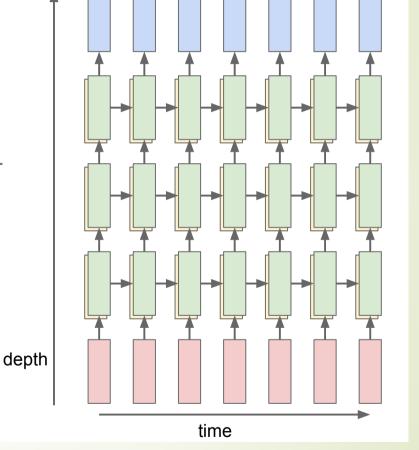
$$h_t^l = \tanh W^l \begin{pmatrix} h_t^{l-1} \\ h_{t-1}^l \end{pmatrix}$$

$$h \in \mathbb{R}^n \quad W^l \quad [n \times 2n]$$

#### LSTM:

$$W^l \ [4n \times 2n]$$

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \operatorname{sigm} \\ \operatorname{sigm} \\ \operatorname{sigm} \\ \tanh \end{pmatrix} W^l \begin{pmatrix} h_t^{l-1} \\ h_{t-1}^{l} \end{pmatrix}$$
$$c_t^l = f \odot c_{t-1}^l + i \odot g$$
$$h_t^l = o \odot \tanh(c_t^l)$$



#### Other RNN Variants

**GRU** [Learning phrase representations using rnn encoder-decoder for statistical machine translation, Cho et al. 2014]

$$r_t = \sigma(W_{xr}x_t + W_{hr}h_{t-1} + b_r)$$

$$z_t = \sigma(W_{xz}x_t + W_{hz}h_{t-1} + b_z)$$

$$\tilde{h}_t = \tanh(W_{xh}x_t + W_{hh}(r_t \odot h_{t-1}) + b_h)$$

$$h_t = z_t \odot h_{t-1} + (1 - z_t) \odot \tilde{h}_t$$

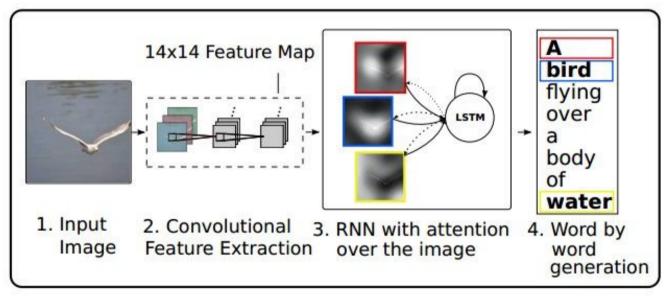
[LSTM: A Search Space Odyssey, Greff et al., 2015]

[An Empirical Exploration of Recurrent Network Architectures, Jozefowicz et al., 2015]

# MUT1: $z = \operatorname{sigm}(W_{xx}x_{t} + b_{z})$ $r = \operatorname{sigm}(W_{xr}x_{t} + W_{hr}h_{t} + b_{r})$ $h_{t+1} = \operatorname{tanh}(W_{hh}(r \odot h_{t}) + \operatorname{tanh}(x_{t}) + b_{h}) \odot z$ $+ h_{t} \odot (1 - z)$ MUT2: $z = \operatorname{sigm}(W_{xx}x_{t} + W_{hx}h_{t} + b_{z})$ $r = \operatorname{sigm}(x_{t} + W_{hr}h_{t} + b_{r})$ $h_{t+1} = \operatorname{tanh}(W_{hh}(r \odot h_{t}) + W_{xh}x_{t} + b_{h}) \odot z$ $+ h_{t} \odot (1 - z)$ MUT3: $z = \operatorname{sigm}(W_{xx}x_{t} + W_{hx} \operatorname{tanh}(h_{t}) + b_{z})$ $r = \operatorname{sigm}(W_{xx}x_{t} + W_{hr}h_{t} + b_{r})$ $h_{t+1} = \operatorname{tanh}(W_{hh}(r \odot h_{t}) + W_{xh}x_{t} + b_{h}) \odot z$

+ h<sub>t</sub> ⊙ (1 - z)

RNN focuses its attention at a different spatial location when generating each word



Xu et al, "Show, Attend, and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015
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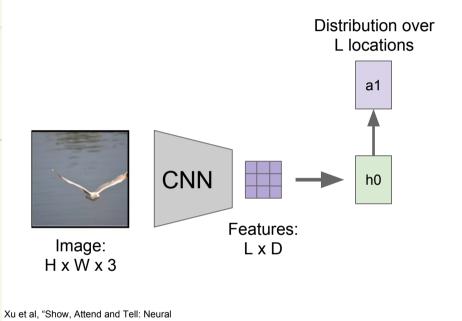
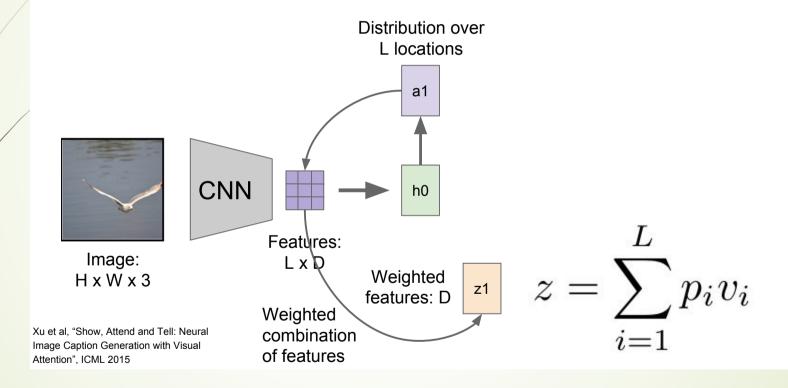
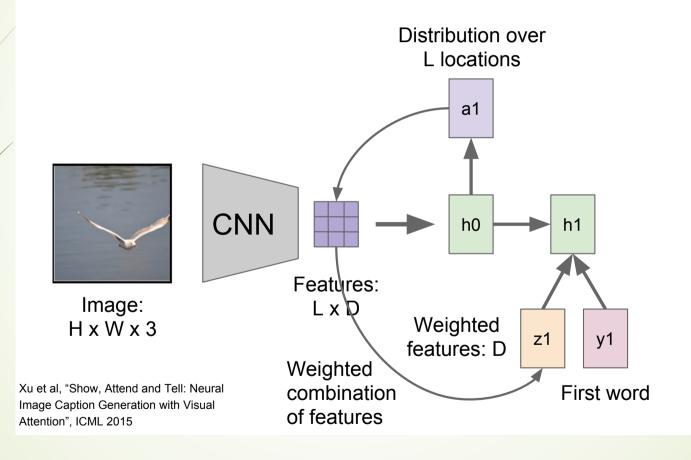
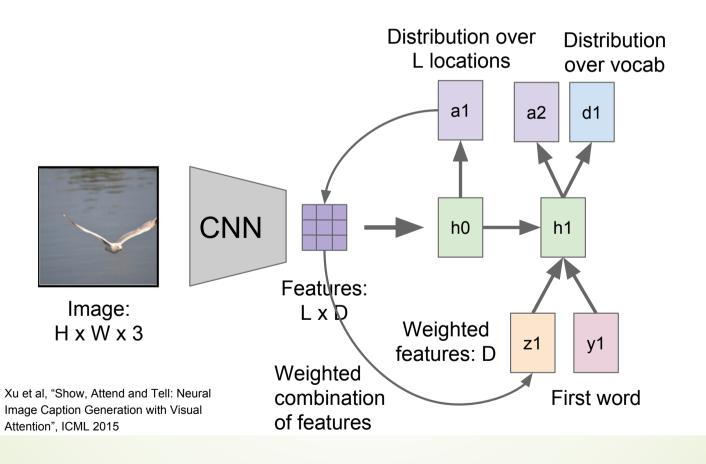


Image Caption Generation with Visual

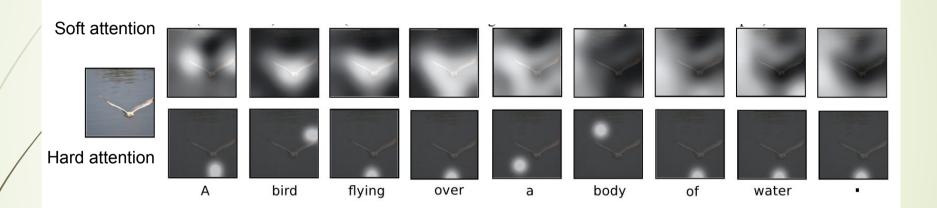
Attention", ICML 2015







#### Image Captioning with Attention Distribution over Distribution Liocations over vocab a1 a2 d1 а3 d2 CNN h1 h0 h2 Features: Image: LxL Weighted HxWx3 **z**1 **z**2 y2 y1 features: D Weighted Xu et al, "Show, Attend and Tell: Neural combination First word Image Caption Generation with Visual of features Attention", ICML 2015



Xu et al, "Show, Attend, and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015
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A woman is throwing a frisbee in a park.



A  $\underline{\text{dog}}$  is standing on a hardwood floor.



A <u>stop</u> sign is on a road with a mountain in the background.



A little <u>girl</u> sitting on a bed with a teddy bear.



A group of <u>people</u> sitting on a boat in the water.



A giraffe standing in a forest with <u>trees</u> in the background.

Xu et al, "Show, Attend, and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015
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# Summary

- RNN is flexible in architectures
- Vanilla RNNs are simple but don't work very well
- Common to use LSTM or GRU: their additive interactions improve gradient flow
  - Backward flow of gradients in RNN can explode or vanish.
  - Exploding is controlled with gradient clipping.
  - Vanishing is controlled with additive interactions
- Better/simpler architectures are a hot topic of current research
- Better understanding (both theoretical and empirical) is needed

# Thank you!

